

Mathematics Reference Sheet

Volume

Cylinder: $V = \pi r^2 h$

Pyramid: $V = \frac{1}{3} B h$

Cone: $V = \frac{1}{3} \pi r^2 h$

Sphere: $V = \frac{4}{3} \pi r^3$

Coordinate Geometry

Midpoint formula:

$$\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

Distance formula:

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

Slope: $m = \frac{y_2 - y_1}{x_2 - x_1}, x_2 \neq x_1$

Special Factoring

$$a^2 - b^2 = (a - b)(a + b)$$

$$a^2 + 2ab + b^2 = (a + b)^2$$

$$a^2 - 2ab + b^2 = (a - b)^2$$

$$a^3 + b^3 = (a + b)(a^2 - ab + b^2)$$

$$a^3 - b^3 = (a - b)(a^2 + ab + b^2)$$

Quadratic Formula

For $ax^2 + bx + c = 0$,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Interest

Simple interest Formula:

$$I = prt$$

Interest Formula (compounded n times per year):

$$A = p \left(1 + \frac{r}{n} \right)^{nt}$$

A = Amount after t years.

p = principal

r = annual interest rate

t = time in years

I = Interest

Trigonometric Identities

Pythagorean Theorem: $a^2 + b^2 = c^2$

$$\sin \theta = \frac{\text{opp}}{\text{hyp}}$$

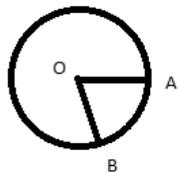
$$\cos \theta = \frac{\text{adj}}{\text{hyp}}$$

$$\tan \theta = \frac{\text{opp}}{\text{adj}}$$

$$\sin^2 \theta + \cos^2 \theta = 1$$

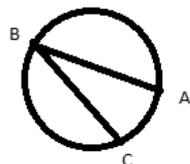
$$\text{Density} = \frac{\text{Mass}}{\text{Volume}}$$

Central Angle



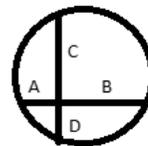
$$m\angle AOB = m\widehat{AB}$$

Inscribed Angle



$$m\angle ABC = \frac{1}{2}m\widehat{AC}$$

Intersecting Chords Theorem



$$A \cdot B = C \cdot D$$

Probability

Permutations: ${}_n P_r = \frac{n!}{(n-r)!}$

Combinations: ${}_n C_r = \frac{n!}{(n-r)!r!}$

Multiplication rule (independent events): $P(A \text{ and } B) = P(A) \cdot P(B)$

Multiplication rule (general): $P(A \text{ and } B) = P(A) \cdot P(B|A)$

Addition rule: $P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$

Conditional Probability: $P(B|A) = \frac{P(A \text{ and } B)}{P(A)}$

Arithmetic Sequence: $a_n = a_1 + (n - 1)d$ where a_n is the n th term, a_1 is the first term, and d is the common difference.

Geometric Sequence: $a_n = a_1 r^{(n-1)}$ where a_n is the n th term, a_1 is the first term, and r is the common ratio.