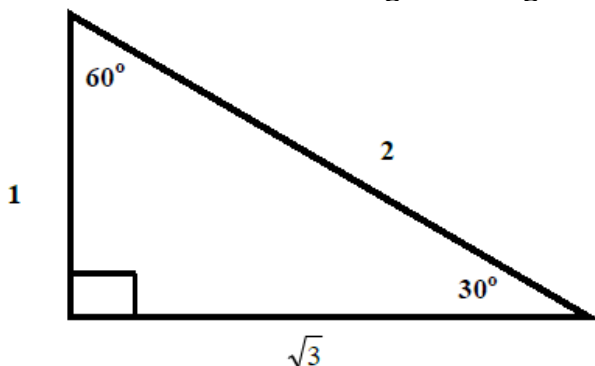


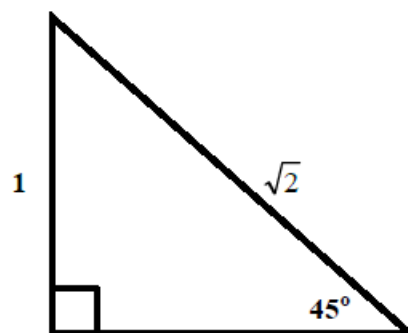
## Trigonometry Fundamentals and the Unit Circle

The six trigonometric functions sine, cosine, tangent, cosecant, secant, cotangent are derived from relationships with right triangles. Common values result from two right triangles:



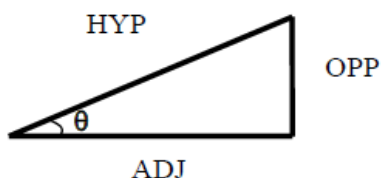
$$\begin{aligned}\sin(30^\circ) &= \frac{\text{OPP}}{\text{HYP}} = \frac{1}{2} \\ \cos(30^\circ) &= \frac{\text{ADJ}}{\text{HYP}} = \frac{\sqrt{3}}{2} \\ \tan(30^\circ) &= \frac{\text{OPP}}{\text{ADJ}} = \frac{1}{\sqrt{3}} = \frac{\sqrt{3}}{3}\end{aligned}$$

(Note: values for  $60^\circ$  are found similarly.)



$$\begin{aligned}\sin(45^\circ) &= \frac{\text{OPP}}{\text{HYP}} = \frac{1}{\sqrt{2}} = \frac{\sqrt{2}}{2} \\ \cos(45^\circ) &= \frac{\text{ADJ}}{\text{HYP}} = \frac{1}{\sqrt{2}} = \frac{\sqrt{2}}{2} \\ \tan(45^\circ) &= \frac{\text{OPP}}{\text{ADJ}} = \frac{1}{1} = 1\end{aligned}$$

### “SOH CAH TOA”



**SOH**  $\sin \theta = \frac{\text{OPP}}{\text{HYP}}$

**CAH**  $\cos \theta = \frac{\text{ADJ}}{\text{HYP}}$

**TOA**  $\tan \theta = \frac{\text{OPP}}{\text{ADJ}}$

**csc**  $\theta = \frac{\text{HYP}}{\text{OPP}}$

**sec**  $\theta = \frac{\text{HYP}}{\text{ADJ}}$

**cot**  $\theta = \frac{\text{ADJ}}{\text{OPP}}$

### “All Students Take Calculus”

Students	All
Sin positive sin: + cos: - tan: -	All positive sin: + cos: + tan: +
Take	Calculus
Tan positive sin: - cos: - tan: +	Cos positive sin: - cos: + tan: -

The Unit Circle – the center at the origin; a radius of 1.

Coordinates of  $(\cos \theta, \sin \theta)$

